

## Cast of Characters

Some Symbols, Functions, and Variables Used in the Book

*Digital Signal Processing and the Microcontroller*

by Dale Grover and John R. Deller

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Symbol	Meaning
$ x $	Function: absolute value of $x$ if $x$ is real; magnitude of $x$ if $x$ is complex (p 33)
$x^*$	Function (superscript asterisk): complex conjugate of the (complex) value $x$ . (Just negate the imaginary part.) (p 195)
$\sum_{i=0}^{N-1} x_i$	Function: summation of elements $x_1, x_2, \dots, x_N$ , i.e., $x_1 + x_2 + \dots + x_N$ (p 123)
\$	Symbol: assembly language prefix indicating a numeric value in hexadecimal (base-16) (p 296)
!	Function: factorial (e.g., $4! = 4 \times 3 \times 2 \times 1 = 24$ ) (p 440)
#	Symbol: assembly language prefix indicating an immediate data value (p 292)
<<	Function: left bit-wise shift (from the C programming language) (p 291)
>>	Function: right bit-wise shift (from the C programming language) (p 291)
$\hat{\phantom{N}}$	Symbol: estimate of variable, as in $\hat{N}$ , an estimate of $N$ (p 168)
$a$	Variable: coefficient of linear congruential generator (a type of pseudo-random number generator) (p 431)
$a_i$	Variable: coefficients of denominator of IIR $H(z)$ , and hence feedback coefficients in IIR filters (p 116, 208)

Symbol	Meaning
A	Variable: parameter of Kaiser window (p 178)
$A_i, B_i$	Variable: IIR filter coefficients (p 321)
$A_{\min}$	Variable: minimum attenuation of a filter (p 127)
$A_p$	Variable: filter passband ripple in dB (p 77)
$A_s$	Variable: filter minimum attenuation in dB (p 77)
b	Variable: bits of resolution in a quantizer (p 119)
$b_i$	Variable: coefficients of numerator of IIR and FIR $H(z)$ , and hence feed-forward coefficients in IIR and FIR filters (p 116, 254)
BW	Variable: bandwidth (e.g., filter) (p 103)
c	Variable: coefficient of linear congruential generator (a type of pseudo-random number generator) (p 431)
C	Variable: capacitance in farads (F) (p 83) Prefix: a capacitor component (e.g., C1 is 10 pF)
$C_N$	Function: Nth order Chebychev polynomial of the first kind (p 217)
dB	Units: decibel, $10 \cdot \frac{P_a}{P_b}$ where $P_a$ and $P_b$ are measures of power (usually in watts). A reference $P_b$ specified by trailing letter, as in dBm, dBV, etc. (p 41)
D	Variable: decimation factor (integer) (p 415)
$e^x$	Function: exponential function. If x is real, just the value e raised to the xth power. If x is complex, see Euler's formula. (p 110 and appendix 1)
f	Variable: discrete-time or normalized frequency, no dimension (p 35)
F	Variable: continuous-time ("real world") frequency measured in Hertz (cycles per second) (p 34) Units: farads, measure of electrical capacitance (p 83)
$F_a$	Variable: aliased frequency (p 98)
$F_c$	Variable: filter passband cutoff or edge frequency in Hz (p 77) Variable: center frequency of bandpass filter in Hz (p 78)
$F_{\text{high}}$ or $F_H,$ $F_{\text{low}}$ or $F_L$	Variable: -3 dB edges of bandpass filter in Hz (p 78)
$F_k$	Variable: frequency associated with kth output of DFT (p 349)

Symbol	Meaning
$F_s$	Variable: filter stopband cutoff or edge frequency in Hz (see also $F_{\text{stop}}$ ) (p 78) Variable: sampling frequency or rate in Hz (p 95)
FS	Variable (full-scale): FSR for ADCs only accepting unipolar ( $\geq 0$ ) inputs (p 120)
FSR	Variable (full-scale range): range of input voltages for an ADC in volts (p 119)
$F_{\text{stop}}$	Variable: alternative notation for filter stopband edge frequency (see $F_s$ ) in Hz (p 78)
G	Prefix: $10^9$ or “giga”, as in GHz
$G_i$	Variable: IIR scaling coefficients (p 321)
$h(t)$	Function: usually the impulse response of a continuous-time system (p 48)
$h_d(n)$	Function: desired impulse response of a system (filter) (p 172)
$H(e^{j\omega})$	Function: (discrete-time) frequency response function (p 108)
$H(j\Omega)$	Function: frequency response or transfer function of a system (p 49)
$H(s)$	Function: system function of a system (p 52)
$H(\Omega)$	Function: Fourier transform of the impulse response of a system, similar to $H(j\Omega)$ (p 55)
$H(z)$	Function: discrete-time system function (p 109)
Hz	Unit: Hertz, i.e. cycles per second. kHz, MHz, GHz. (p 34)
$i$	Variable: current (not $\sqrt{-1}$ !) (p 469)
I	Variable: interpolation factor (integer) (p 418)
$I_0(\cdot)$	Function: zero-order modified Bessel function of the first kind (not really used in this book) (p 181)
$\text{Im}(x)$	Function; the imaginary part of a complex value $x$ (p 33)
$j$	Symbol: the quantity $\sqrt{-1}$ (note that “ $i$ ” is reserved for current in electronics) (p 33)
$j\Omega$	(Symbol): vertical axis of $s$ -plane
k or K	Prefix: $10^3$ or “kilo”, as in kHz

Symbol	Meaning
$l$	Variable (lower case L): lag in correlation (p 384)
$\ln()$	Function: logarithm function base e (i.e., $\ln(e^2)=2$ )
$\log()$	Function: logarithm function, usually taken as base 10 (i.e., $\log(100)=2$ ). See also $\ln()$ , $\log_2()$
$\log_2()$	Function: logarithm function base 2 (i.e., $\log_2(8)=3$ )
$m$	Variable: coefficient of linear congruential generator (a type of pseudo-random number generator) (p 431) Prefix: $10^{-3}$ or “milli”, as in mV (p 124)
$M$	Variable: number of zeros in a comb filter (p 187) Prefix: $10^6$ or “mega”, as in MHz
$N$	Variable: number of samples in a signal (p 123)
$\hat{N}$	Variable: estimate of $N$ , the number of coefficients in an FIR filter (p 168)
$n$	Variable: usually an integer, often an index into a discrete-time signal (p 103)
$n_p$	Variable: number of poles in a system (p 116)
$n_z$	Variable: number of zeros in a system (p 116)
$p$	Variable (often subscripted): a pole of a system (p 86) Prefix: $10^{-12}$ or “pico”, as in pF
$P$	Variable: power, usually in W (watts) (p 41)
$P_N$	Variable: noise power, in watts (p 122)
$P_S$	Variable: signal power, in watts (p 122)
$Q$	Variable: “Quality” factor of bandpass or bandstop filter (no units) (p 79)
$r$	Variable: magnitude of the complex variable $z$ (p 110)
$r_{12}$	Function: crosscorrelation between signals 1 and 2 (p 384)
$r_{xx}$	Function: autocorrelation (p 396)
rad	Unit: radians, an angular measure like degrees (p 34)
$R$	Variable: resistance in ohms ( $\Omega$ ) (p 83) Prefix: a resistor component (e.g., R1 is 100 ohms)
$\text{Re}(x)$	Function: the real part of a complex value $x$ (p 33)

Symbol	Meaning
$s$	Units: seconds (p 35) Variable: a variable in the “s” or complex-frequency plane, $s=\sigma+j\omega$ (p 53)
$s_i$	Variable: scaling terms in IIR filter (p 319)
SNR	Variable (signal to noise ratio): ratio of signal to noise in dB (p 122)
$t$	Variable: time in seconds (p 21)
$t_d$	Variable: time delay in seconds (p 36)
$T$	Variable: period in seconds (p 35)
$T_s$	Variable: sampling period in seconds (p 95)
$V$	Variable: voltage (electrical potential) in V (volts) (p 42)
$w(n)$	Function (“w”, not $\omega$ !): window function (p 179) Variable: intermediate storage variables in IIR filter (p 254)
$W_N$	Variable: “twiddle” factors in DFT, FFT (p 355)
$x(n)$	Function: discrete-time input of a system (p 116)
$x(t)$	Function: continuous-time (input) signal (p 58)
$X(k)$	Function: frequency domain output of DFT/FFT (p 354)
$X(z), Y(z)$	Function: z-transform of the input and output signals of a discrete-time system (p 111)
$y(n)$	Function: discrete-time output of a system (p 116)
$y(t)$	Function: continuous-time (output) signal (p 58)
$z_i$	Variable: a zero of a system (p 86)
$z$	Variable: variable in the z or discrete-time complex frequency plane (p 109)
$z^{-1}$	(Symbol): a delay of one sample period in a discrete-time system (p 153)
$Z$	Variable: impedance, a complex-valued, often frequency-dependent electrical measure (p 84)
$\beta$	Variable: parameter of Kaiser window (p 178)
$\delta(t)$	Function (lower case delta): impulse function (p 48)
$\delta_m$	Variable: minimum stopband attenuation in a window function (p 182)
$\delta_p$	Variable (lower case delta): filter passband deviation (p 77)

Symbol	Meaning
$\delta_s$	Variable (lower case delta): filter stopband ripple (p 77)
$\Delta$	Variable: step size in an analog-to-digital quantizer (p 119)
$\Delta f$	Variable: width of transition band in a filter, e.g., $f_s - f_p$ (p 168)
$\Delta x$	Variable: increment in radians between table entries in a first-order sine table (p 444)
$\varepsilon$	Variable: error in polynomial estimate of the sine function (p 444)
$\varepsilon_p$	Variable (lower case epsilon): alternative expression of filter passband deviation (p 77)
$\mu$	Prefix: $10^{-6}$ or “micro”, as in $\mu\text{V}$ (p 124)
$\pi$	Symbol (lower-case “pi”): the constant 3.14159265... (p 34)
$\theta$	Variable (lower-case “theta”): usually an angle or phase angle (p 33)
$\rho_{12}$	Function (lower case rho): normalized crosscorrelation (p 385)
$\sigma$	Variable (lower case sigma): exponential factor in complex frequency (see “s”) (p 53) Symbol: horizontal axis of s-plane
$\tau$	Variable (lower case tau): time constant in seconds (p 125)
$\tau_a$	Variable: aperture time in a sample and hold amplifier (p 132)
$\omega$	Variable (lower case omega--not “w”!): discrete-time or normalized frequency, units of radians (p 35)
$\Omega$	Variable (upper-case “omega”): continuous-time (“real world”) frequency measured in radians per second (p 34) Units: ohms, measure of electrical resistance (p 83)
$\Omega_c$	Variable (upper case omega): filter passband cutoff or edge frequency in rad/sec (p 77) Variable: center frequency of bandpass filter in rad/sec (p 78)
$\Omega_s$	Variable (upper case omega): filter stopband cutoff or edge frequency in rad/sec (p 78) Variable: sampling frequency or rate in rad/sec (p 95)
$\infty$	Symbol: infinity (p 77)
$\propto$	Symbol: “is proportional to” (p 40)
$\angle x$	Function: angle of complex value x (p 33) Symbol: quantity that follows is an angle (often in radians) (p 33)